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STEP500

S/198/62/008/005/005/009 D234/D308

SAUTHOR: (§)

Mindin, O. A.

ITITLE:

Theory of motion of bodies of variable mass in relativistic version

PERIODICAL: Akademiya nauk Ukrayins'koyi RSR. Instyut mekhaniky. Prikladna mekhanika, v. 8 ... 5, 1962, 546-551

TEXT: The author considers the motion in the absence of external forces, assuming that the fuel mass dm used during a time dt is split into two parts, which he calles defect mass dm and slag mass dm. One part of dm is converted into electromagnetic radiation and the other is used for disposing of dm. Velocities close to the velocity of light are considered. The basic equations of motion are taken from a paper by V. F. Kotov. Using the relativistic formula of addition of velocities, the author obtains the differential equation of the problem, whose solution is

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. Theory of motion ...

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$$\frac{M_{e}}{M_{eO}} = B \sqrt{\frac{F(v)}{F(O)}} \frac{f(O)}{f(v)}$$

(1.7)

where M_e denotes the rest mass of the body, $\beta = v/c$.

$$\Delta = -\left\{4u_{\mathbf{r}}c^{2}\left[\alpha\varepsilon c + (1-\varepsilon)u_{\mathbf{r}}\right] + \varepsilon^{2}c^{2}(\alpha u_{\mathbf{r}} - c)^{2}\right\}$$

$$u_r v^2 + (\alpha u_r - c) \varepsilon c v - c^2 \left[\alpha \varepsilon c + (1-\varepsilon) u_r\right] = f(v)$$

* V. F. Kotovi, Theory of New Rocket Types, Odessa Cout. Inst. im.
J. J. Hechnikov, Math Science Series, 146, 6, 1956.

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Theory of motion ...

$$\frac{2u_{\mathbf{r}}v + \varepsilon c(\alpha u_{\mathbf{r}} - c) - \sqrt{-\Delta}}{2u_{\mathbf{r}}v + \varepsilon c(\alpha u_{\mathbf{r}} - c) + \sqrt{-\Delta}} = F(v); \frac{c[(2 - \varepsilon)c + \varepsilon \alpha u_{\mathbf{r}}]}{\sqrt{-\Delta}} = \delta$$

ur is the relative velocity with which the slag mass is ejected, is the radiation coefficient and £ the mass defect coefficient, the initial values are

$$M_e = M_{e0}; v = 0; f(v) = f(0); F(v) = F(0)$$

An implicit formula is obtained for the final velocity of the body, when the fuel has been consumed. For u

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Theory of motion ...

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$$u_{\mathbf{r}} = c \left\{ 1 - \left[\frac{1 - \varepsilon}{\varepsilon (1 - \alpha) + (1 - \varepsilon)} \right]^{2} \right\}^{\frac{1}{2}}$$
(2.2)

is derived. When $\alpha=\epsilon=1$, $u_r=0$, a differential equation is obtained which was solved by Kotov. When v^2/c^2 is small, another result of Kotov is obtained.

ASSOCIATION: Odes'kyy derzhavnyy universytet (Odessa State University)

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